MS-HGAT: Memory-enhanced Sequential Hypergraph Attention Network for Information Diffusion Prediction

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Code: https://github.com/slingling/MS-HGAT





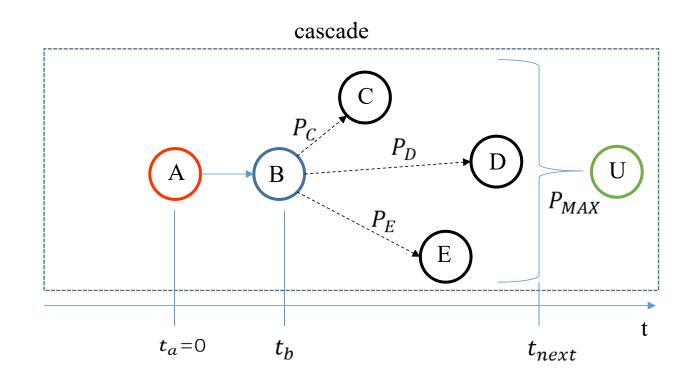
Introduction

Using the friendship network is insufficient to describe users' interactive preferences.

Ignored the dynamic connections between users and cascades

Taking advantages of both the friendships and diffusion interactions of users.

Proposing a sequential hypergraph attention network to learn the short-term interactions between users and cascades



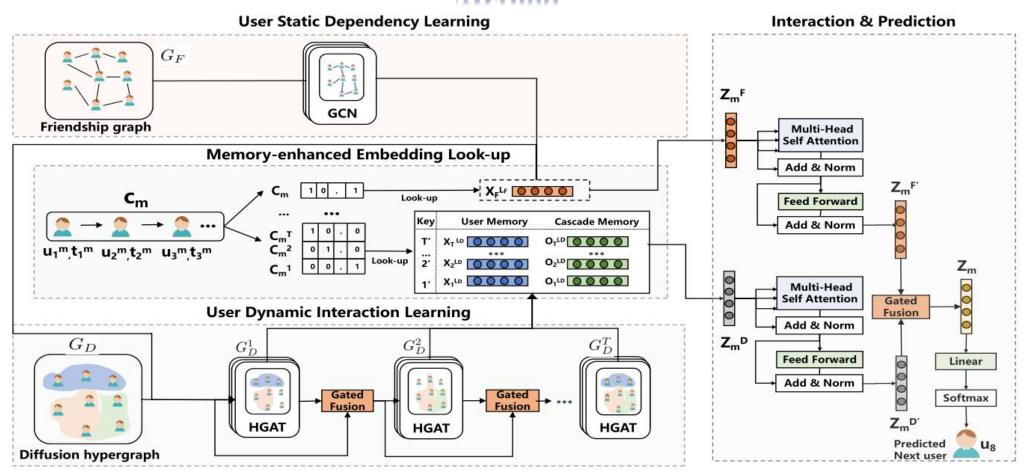


Figure 1: Four modules of MS-HGAT: 1) users' friendships are learned by GCN in user static dependency learning module; 2) user dynamic interaction learning module obtains interaction-based user and cascade embeddings through sequential HGATs; 3)memory-enhanced embedding look-up refers to finding the corresponding representation vectors in the static user representation and the dynamic memory block; 4)in interaction & prediction module, self-attention mechanisms are used to efficiently interact features in cascade, finally, probability of infection of candidates is calculated by Softmax function.

Problem Formulation

User set: $U = \{u_1, u_2, ..., u_n\}$

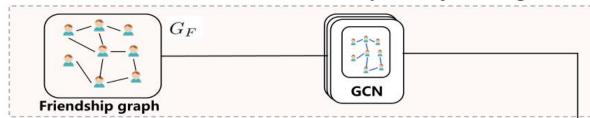
friendship graph: $G_F = (U, E)$

historical diffusion cascades: $C = \{c_1, c_2, \dots, c_M\}$ |C| = M

diffusion hypergraphs: $G_D = \{G_D^t | t = 1, 2, ..., T\}$ $G_D^t = (U^t, \mathcal{E}^t)$

diffusion sequence: $c_m = \{(u_i^m, t_i^m) | u_i^m \in U\}$

User Static Dependency Learning



User Static Dependency Learning

$$\mathbf{X}_{F}^{l+1} = \sigma \left(\tilde{\mathbf{D}_{F}}^{-\frac{1}{2}} \tilde{\mathbf{A}_{F}} \tilde{\mathbf{D}_{F}}^{-\frac{1}{2}} \mathbf{X}_{F}^{l} \mathbf{W}_{F} \right)$$

$$\mathbf{X}_{F}^{0} \in \mathbb{R}^{N \times d}$$

$$\tilde{A}_{F} = A_{F} + I$$

$$(1)$$

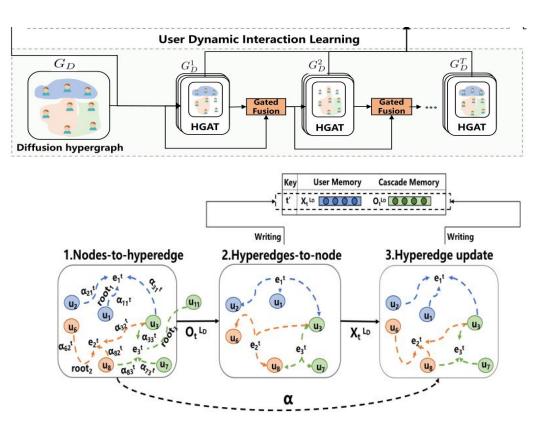


Figure 2: Stages of HGAT: (1) nodes-to-hyperedge aggregation, the root node of each cascade is determined in advance for attention calculation; (2) hyperedges-to-node aggregation, each hyperedge shares the same weight in this operation; (3) hyperedge update, the attention coefficient α is retained from first nodes-to-hyperedge aggregation. The learned user and the cascade representations are separately written to the memory module.

User Dynamic Interaction Learning: HGAT

Nodes-to-hyperedge aggregation:

$$\mathbf{o}_{j,t}^{l+1} = \sigma(\sum_{u_i^t \in e_j^t} \alpha_{ij}^t \mathbf{W}_1 \mathbf{x}_{i,t}^l)$$
 (2)

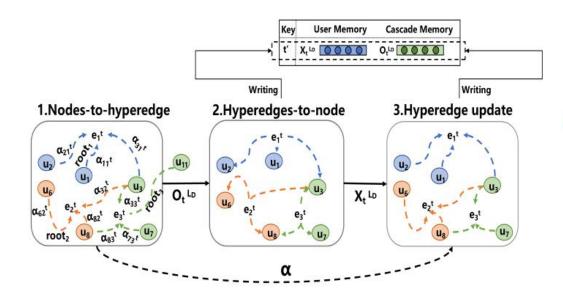
$$\alpha_{ij}^{t} = \frac{\exp(-\operatorname{dis}(\mathbf{W}_{1}\mathbf{x}_{i,t}^{l}, \mathbf{W}_{1}\mathbf{r}_{j}^{l}))}{\sum_{u_{p}^{t} \in e_{j}^{t}} \exp(-\operatorname{dis}(\mathbf{W}_{1}\mathbf{x}_{p,t}^{l}, \mathbf{W}_{1}\mathbf{r}_{j}^{l}))}$$
(3)

Hyperedges-to-node aggregation:

$$\mathbf{x}_{i,t}^{l+1} = \sigma(\sum_{e_j^t \in \mathcal{E}_i^t} \mathbf{W}_2 \mathbf{o}_{j,t}^{l+1})$$
(4)

Update of hyperedges:

$$\mathbf{o}_{j,t}^{l+1'} = \sigma(\sum_{u_i^t \in e_j^t} \alpha_{ij}^t \mathbf{W}_3 \mathbf{x}_{i,t}^{l+1})$$
 (5)



Sequential HGATs with Gated Fusion Strategy

$$\mathbf{x}_{i,t+1}^{0} = g_{R_{1}}\mathbf{x}_{i,t}^{L_{D}} + (1 - g_{R_{1}})\mathbf{x}_{i,t}^{0}$$

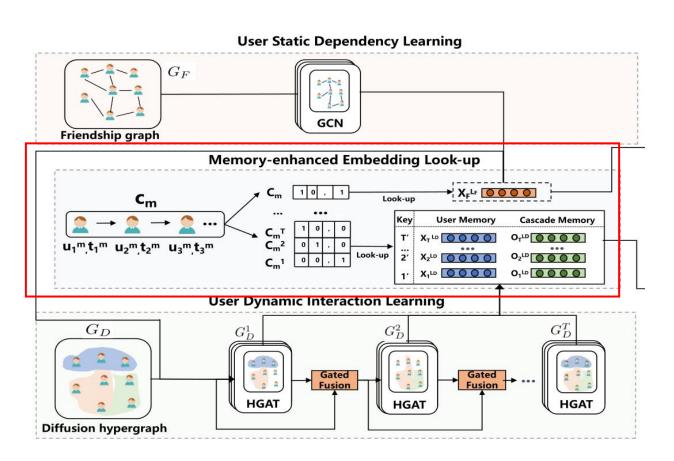
$$g_{R_{1}} = \frac{\exp(\mathbf{W}_{Z_{1}}^{T}\sigma(\mathbf{W}_{R_{1}}\mathbf{x}_{i,t}^{L_{D}}))}{\exp(\mathbf{W}_{Z_{1}}^{T}\sigma(\mathbf{W}_{R_{1}}\mathbf{x}_{i,t}^{L_{D}})) + \exp(\mathbf{W}_{Z_{1}}^{T}\sigma(\mathbf{W}_{R_{1}}\mathbf{x}_{i,t}^{0}))}$$

$$\mathbf{X}_{1}^{0} = \mathbf{X}_{F}^{L_{F}}$$
(7)

Memory Module

$$M_D = \left\{ t' : (X_t^{L_D}, O_t^{L_D}) \right\}, t = 1, 2, ..., T$$
 (6)

Memory-enhanced Embedding Look-up



Static representation look up:

Given the target cascade: $c_m = \{(u_i^m, t_i^m) | u_i^m \in U\}$

$$Z_{\mathbf{m}}^F = [(\mathbf{x}_i)] \in R^{|c_m| \times d} i = 0, 1, \dots, \mathcal{N}-1.$$

Static representation look up:

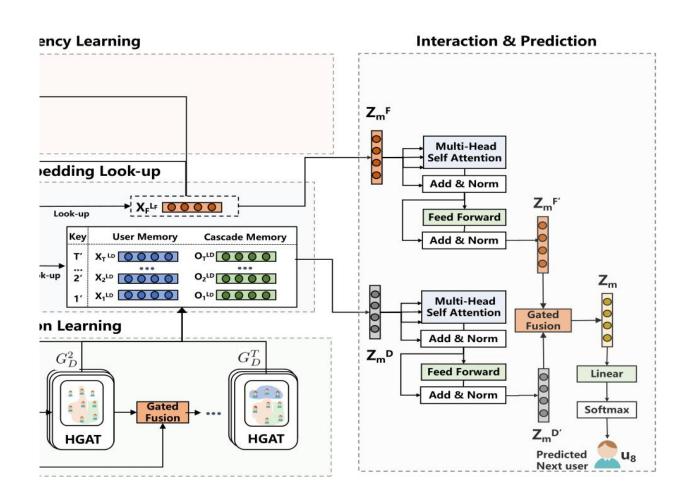
if
$$t_i^m \ge t'$$
 and $t_i^m < (t+1)' \longrightarrow x_{i,t} \leftarrow X_t^{L_D}$

$$q_{\mathbf{m}}^{D} = [(\mathbf{x}_{i,t})] \in R^{|c_m| \times d} \quad i=0,1,\cdots,\mathcal{N}-1, t=1,2,\cdots,\mathcal{T}.$$

$$p_{\mathbf{m}}^F = [(o_{m,t})] \in R^{|c_m| \times d} \quad t=1,2,\cdots,T.$$

$$\mathbf{Z}_m^D = g_{R_2} \mathbf{p}_m^D + (1 - g_{R_2}) \mathbf{q}_m^D$$

$$g_{R_2} = \frac{\exp(\mathbf{W}_{Z_2}^T \sigma(\mathbf{W}_{R_2} \mathbf{p}_m^D)}{\exp(\mathbf{W}_{Z_2}^T \sigma(\mathbf{W}_{R_2} \mathbf{p}_m^D) + \exp(\mathbf{W}_{Z_2}^T \sigma(\mathbf{W}_{R_2} \mathbf{q}_m^D)})$$
(8)



Feature Interaction & Prediction

Self-attention:

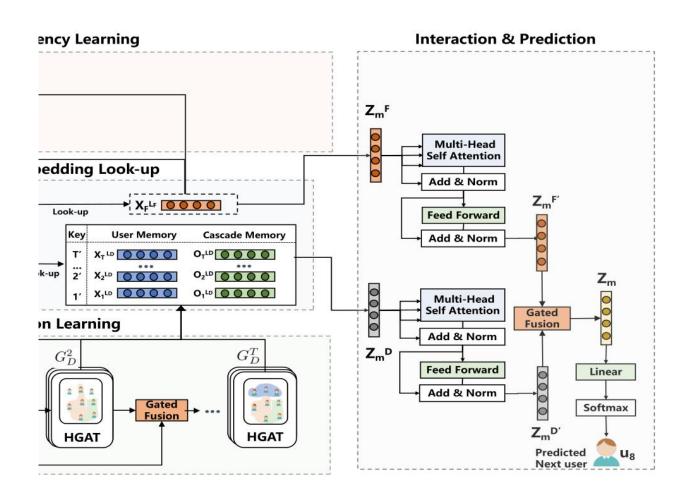
Att(
$$\mathbf{Q}, \mathbf{K}, \mathbf{V}$$
) = softmax $\left(\frac{\mathbf{Q}\mathbf{K}^{T}}{\sqrt{d'}} + \mathbf{M}\right) \mathbf{V}$
 $\mathbf{h}_{i,m}^{F} = \text{Att}\left(\mathbf{Z}_{m}^{F}\mathbf{W}_{i}^{Q}, \mathbf{Z}_{m}^{F}\mathbf{W}_{i}^{K}, \mathbf{Z}_{m}^{F}\mathbf{W}_{i}^{V}\right)$ (9)
 $\mathbf{h}_{m}^{F} = \left[\mathbf{h}_{1,m}^{F}; \mathbf{h}_{2,m}^{F}; \dots; \mathbf{h}_{H,m}^{F}\right] \mathbf{W}^{O}$
 $M \in \mathbb{R}^{|c_{m}| \times |c_{m}|}$
 $M_{i,j} = -\infty \text{ if } i > j \text{ else } M_{i,j} = 0$
 $\mathbf{Z}_{m}^{F'} = \text{ReLU}\left(\mathbf{h}_{m}^{F}\mathbf{W}_{A_{1}} + \mathbf{b}_{1}\right) \mathbf{W}_{A_{2}} + \mathbf{b}_{2}$ (10)

Fusion Layer:

$$\mathbf{Z}_{m} = g_{R_{3}} \mathbf{Z}_{m}^{D'} + (1 - g_{R_{3}}) \mathbf{Z}_{m}^{F'}$$

$$g_{R_{3}} = \frac{\exp(\mathbf{W}_{Z_{3}}^{T} \sigma(\mathbf{W}_{R_{3}} \mathbf{Z}_{m}^{D'})}{\exp(\mathbf{W}_{Z_{3}}^{T} \sigma(\mathbf{W}_{R_{3}} \mathbf{Z}_{m}^{D'}) + \exp(\mathbf{W}_{Z_{3}}^{T} \sigma(\mathbf{W}_{R_{3}} \mathbf{Z}_{m}^{F'})}$$

$$(11)$$



Diffusion Prediction:

$$\hat{y} = \operatorname{softmax}(\mathbf{W}_{p}\mathbf{Z}_{m} + \mathbf{Mask}_{m})$$

$$(\mathbf{Mask}_{m})_{1,i}^{j,i} = 0$$

$$(\mathbf{Mask}_{m})_{i+1,i}^{|c_{m}|,i} = -\infty$$

$$(12)$$

$$\mathcal{J}(\theta) = -\sum_{j=2}^{|c_m|} \sum_{i=1}^{|U|} \mathbf{y}_{ji} \log \left(\hat{\mathbf{y}}_{ji}\right)$$
 (13)

in which θ represents all parameters that need to be learned in the model, if the user u_i participate in cascade c_m at the step j, $\mathbf{y}_{ii} = 1$, otherwise $\mathbf{y}_{ii} = 0$.

Table 1: Statistics of datasets used in our experiments

Datasets	Twitter	Douban	Android	Christ.		
# Users	12,627	12,232	9,958	2,897		
	**	Frienship		71		
# Links	309,631	396,580	48,573	35,624		
Density	24.52	30.21	4.87	12.30		
		Interaction				
# Cascades	3,442	3,475	679	589		
Avg. Length	32.60	21.76	33.3	22.9		
Density	8.89	6.18	2.27	4.66		

Table 2: Experimental results on 4 dataset (%) (Hits@k scores for K = 10, 50, 100), scores are the higher the better.

Models	Twitter		Douban		Android			Christianity				
	@10	@50	@100	@10	@50	@100	@10	@50	@100	@10	@50	@100
DeepDiffuse	5.79	10.80	18.39	9.02	14.93	19.13	4.13	10.58	17.21	10.27	21.83	30.74
Topo-LSTM	8.45	15.80	25.42	8.57	16.53	21.47	4.56	12.63	16.53	12.28	22.63	31.52
NDM	15.21	28.23	32.30	10.00	21.13	30.14	4.85	14.24	18.97	15.41	31.36	45.86
SNIDSA	25.37	36.64	42.89	16.23	27.24	35.59	5.63	15.22	20.93	17.74	34.58	48.76
FOREST	28.67	42.07	49.75	19.50	32.03	39.08	9.68	17.73	24.08	24.85	42.01	51.28
Inf-VAE	14.85	32.72	45.72	8.94	22.02	35.72	5.98	14.70	20.91	18.38	38.50	51.05
DyHGCN	31.88	45.05	52.19	18.71	32.33	39.71	9.10	16.38	23.09	26.62	42.80	52.47
MS-HGAT (ours)	33.50	49.59	58.91	21.33	35.25	42.75	10.41	20.31	27.55	28.80	47.14	55.62
recurrence	33.38	49.49	58.98	22.19	35.64	43.11	10.85	20.23	27.76	28.00	47.33	56.60

Table 3: Experimental results on 4 dataset (%) (MAP@k scores for K = 10, 50, 100), scores are the higher the better.

Models	Twitter		Douban			Android			Christianity			
	@10	@50	@100	@10	@50	@100	@10	@50	@100	@10	@50	@100
DeepDiffuse	5.87	6.80	6.39	6.02	6.93	7.13	2.30	2.53	2.56	7.27	7.83	7.84
Topo-LSTM	8.51	12.68	13.68	6.57	7.53	7.78	3.60	4.05	4.06	7.93	8.67	9.86
NDM	12.41	13.23	14.30	8.24	8.73	9.14	2.01	2.22	2.93	7.41	7.68	7.86
SNIDSA	15.34	16.64	16.89	10.02	11.24	11.59	2.98	3.24	3.97	8.69	8.94	9.72
FOREST	19.60	20.21	21.75	11.26	11.84	11.94	5.83	6.17	6.26	14.64	15.45	15.58
Inf-VAE	19.80	20.66	21.32	11.02	11.28	12.28	4.82	4.86	5.27	9.25	11.96	12.45
DyHGCN	20.87	21.48	21.58	10.61	11.26	11.36	6.09	6.40	6.50	15.64	16.30	16.44
MS-HGAT (ours)	22.49	23.17	23.30	11.72	12.52	12.60	6.39	6.87	6.96	17.44	18.27	18.40
recurrence	21.15	21.83	21.96	12.09	12.72	12.83	6.51	6.97	7.07	17.19	18.06	18.21

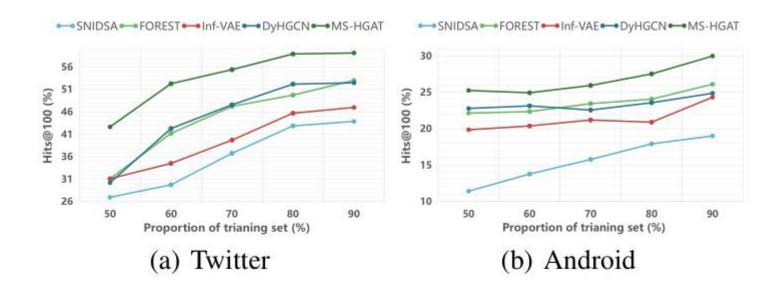


Figure 3: Impact of training proportion.

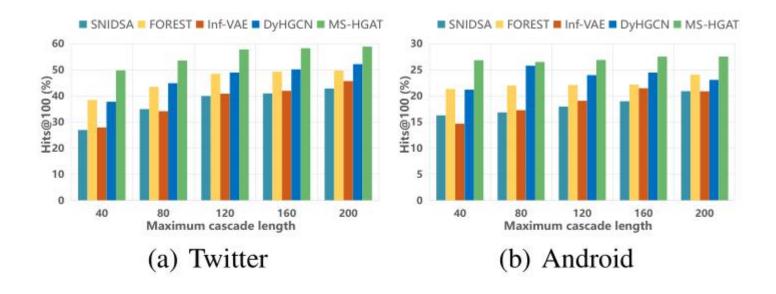


Figure 4: Impact of maximum cascade lengths.

Table 4: Ablation study of MS-HGAT.

Models MS-HGAT	Twi	itter	Android			
	Hits@100	MAP@100	Hits@100	MAP@100 6.96		
	58.91	23.30	27.55			
w/o FG	57.20	21.38	26.32	6.86		
w/o DH	57.41	22.24	26.74	6.78		
w/o UM	58.63	22.74	26.40	6.83		
w/o CM	58.32	21.96	27.09	6.77		
w/o ATTH	58.95	22.76	27.03	6.75		
w/o GF	57.93	22.19	27.26	6.89		

Thanks